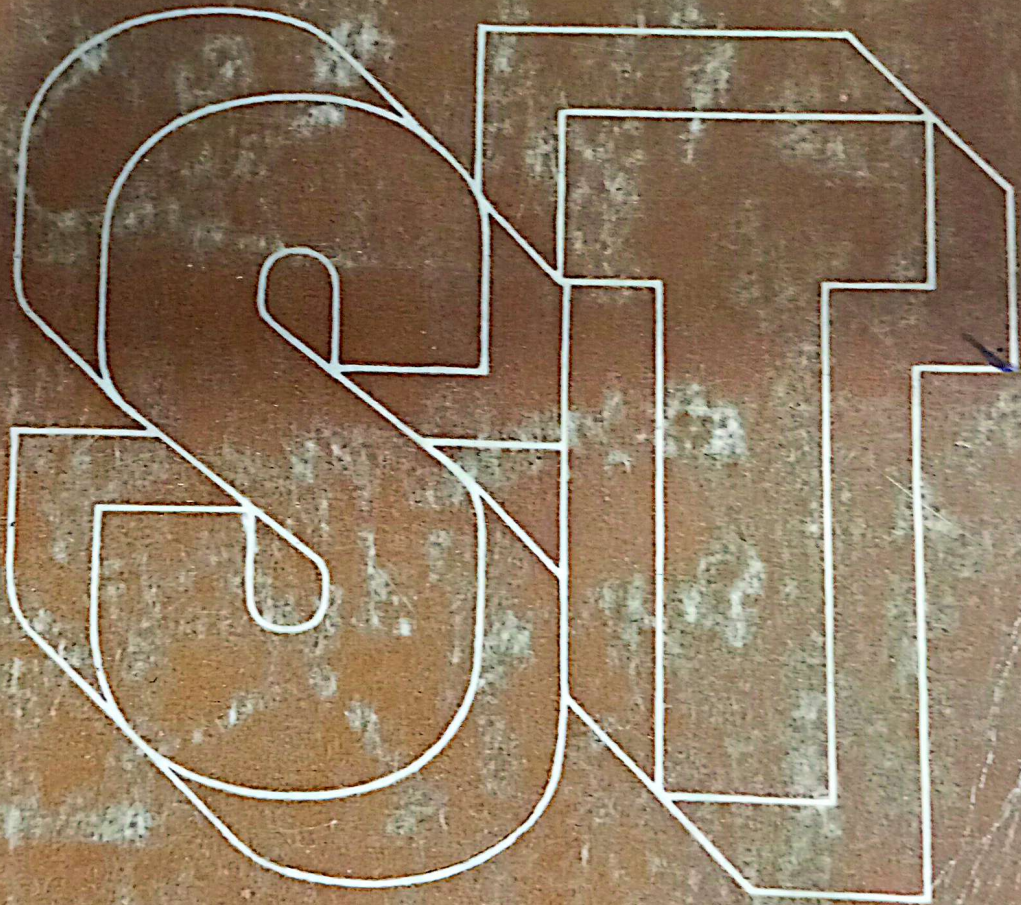


Quantum Theory of Solids

Edited by I. M. LIFSHITS

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CONTENTS

Foreword 5

1	DEFECTS AND SURFACE PHENOMENA IN QUANTUM CRYSTALS BY A. F. ANDREEV (<i>transl. by E. Yankovsky</i>)	11
	Introduction	11
1.1	Quantum Effects in Crystals	11
1.2	Impurity Quasiparticles: Impuritons	14
1.3	Diffusion in an Impuriton Gas	14
1.3.1	Diffusion of Strongly Interacting Impuritons	17
1.3.2	Phonon-Impuriton Interaction	20
1.3.3	One- and Two-Dimensional Impuritons	24
1.3.4	Vacancies	32
1.4.	Vacancies in ^4He Crystals	32
1.4.1	Zero-Point Vacancies	37
1.4.2	Vacancies in ^3He Crystals	40
1.4.3	Surface Phenomena	42
1.5.	The Equilibrium Shape of the Crystal-Liquid Interface	42
1.5.1	Crystallization and Melting	48
1.5.2	Crystallization Waves	51
1.5.3	Faceting Transitions in Crystals	55
1.6	The Role of Fluctuations	55
1.6.1	Thermodynamic Relations	58
1.6.2	A 6-fold Symmetry Axis	60
1.6.3	A 4-fold Symmetry Axis	61
1.6.4	Delocalization of Dislocations	64
1.7	References	66

ELECTRONIC PHASE TRANSITIONS AND THE PROBLEM OF MIXED VALENCE BY D. I. KHOMSKII (*transl. by E. Yankovsky*) 70

2.1	Introduction	70
2.2	Localization of Electrons and Insulator-Metal Transitions (Mott-Hubbard Transitions)	72
2.3	Electronic Phase Transitions in Rare-Earth Compounds	75
2.3.1	The General Picture of Transitions	75

2.3.2	Theoretical Models for Describing Electronic Phase Transitions and MV States	77	
2.4	Valence Transitions in the Falicov-Kimball Model	80	
2.4.1	The Mean-Field Approximation	80	3.4.1
2.4.2	Beyond the Mean-Field Approximation. The Role of Local (Excitonic) Correlations	84	3.4.2
2.4.3	The Two-Level Model	87	3.4.3
2.4.4	The Periodic Model	89	3.4.4
2.5	The Electron-Lattice Interaction and Its Role in Transitions	91	3.5
2.5.1	Interaction with a Homogeneous Strain	91	3.6
2.5.2	The Change in the Width of the f Level and Its Role in Valence Transitions	97	3.6.1
2.5.3	Local (Polaron) Effects in the Electron-Lattice Interaction	99	3.6.2
2.5.4	Interaction via Short-Wavelength Phonons and Formation of Ordered Structures	102	3.6.3
2.6	Mixed-Valence States: The Basic Problems	105	3.7
2.6.1	Properties of Mixed-Valence States. The Experimental Situation and Statement of the Problem	106	3.7.1
2.6.2	The Anderson and Kondo Lattices	109	3.7.2
2.6.3	The Valence Transition and the Mott-Hubbard Transition	114	3.7.3
2.6.4	Excitonic Correlations in an MV Phase	117	3.7.4
2.6.5	Spatial Correlations in MV Systems	119	3.7.5
2.6.6	Systems with MV as a Model of Condensed Matter	121	3.7.6
2.7	Conclusion	123	3.7.7
	References	126	3.7.8
3	COHERENT EFFECTS IN DISORDERED CONDUCTORS BY B. L. ALTSHULER, A. G. ARONOV, D. E. KHMELNITSKII AND A. I. LARKIN (<i>transl. by E. Kaminskaya</i>)	130	3.8
3.1	Introduction	130	3.8.1
3.2	Quantum Corrections to Conductivity of Noninteracting Electrons	131	3.8.2
3.2.1	Conductivity and Impurity Diagrammatic Technique	131	3.8.3
3.2.2	Cooperon and Quantum Correction to Conductivity	134	3.8.4
3.2.3	Effects of Spin Scattering	137	3.8.5
3.2.4	Properties of Samples of Finite Dimensions. Effective Space Dimensionality	142	3.8.6
3.3	Quantum Effects in High-Frequency Electromagnetic Field	144	3.8.7
3.3.1	Effects of High-Frequency Field on Quantum Corrections to Conductivity	144	3.8.8
3.3.2	Suppression of Coherent Effects by Electromagnetic Fluctuations	146	3.8.9
3.4	Electron-Electron Interaction in Disordered Metallic Systems	151	3.9

Contents

9

3.4.1	Electron-Electron Collision Time 151
3.4.2	Effects of Electron-Electron Correlations on the Density of One-Particle States 160
3.4.3	Conductivity of Interacting Electrons 170
3.4.4	Superconducting Fluctuations and Temperature Dependence of Conductivity 176
3.5	Temperature Dependence of Conductivity: Experiment 179
3.6	Hall Effect 187
3.6.1	Introduction 187
3.6.2	Hall Effect for Noninteracting Electrons 188
3.6.3	Hall Effect for Interacting Electrons 189
3.7	Anomalous Magnetoresistance 191
3.7.1	Magnetoresistance of Noninteracting Electrons 191
3.7.2	Magnetoresistance of Thin Films and Wires in Longitudinal Magnetic Field 194
3.7.3	Magnetoresistance and Scattering by Superconducting Fluctuations 196
3.7.4	Magnetoresistance in Many-Valley Semiconductors 197
3.7.5	Effects of Spin-Orbit Scattering on Magnetoconductivity 199
3.7.6	Experiment 202
3.7.7	Aharonov-Bohm Effect in Disordered Metals 206
3.7.8	Effects of Electron-Electron Interaction in Magnetic Field 208
3.8	Electron Localization in Random Potential 213
3.8.1	Analogy Between Electron Properties in Disordered Systems and Statistical Mechanics of Ferromagnets 213
3.8.2	Q-Hamiltonian 214
3.8.3	Renormalization Group Equation 216
3.8.4	Conductivity in Two Dimensions 217
3.8.5	Localization in One and Three Dimensions 219
3.8.6	Localization in Magnetic Field 222
3.8.7	Localization in Percolating Structures 223
3.9	Conclusion 225
3.A	Appendices 226
3.A.1	Cooperon-Current Relation in the Space-Time Representation 226
3.A.2	Cooperon in External Electromagnetic Field 229
3.A.3	Calculation of Path Integrals 230
3.A.4	Expression for Conductivity of Interacting Electrons 232
	References 235

4

AN EXACT SOLUTION OF THE KONDO PROBLEM BY P.B. WIEGMANN (transl. by E. Yankovsky) 238

4.1

Introduction 238

4.2

The Basic Models 244

4.2.1

The Anderson Model 245

4.2.2	The Angular Dependence of Hybridization Amplitudes. A One-Dimensional Hamiltonian	246
4.2.3	Hierarchy of Energies	247
4.2.4	Exchange Hamiltonians	248
4.2.5	The Simple Exchange Hamiltonians	250
4.2.6	Perturbation Theory	254
4.3	Bethe's Method	257
4.3.1	General Survey. The Factorization Equations	257
4.3.2	An Effective Hamiltonian	263
4.3.3	The Bethe Ansatz for the s-d Exchange Model	264
4.3.4	Periodic Boundary Conditions	269
4.3.5	The Set of Commuting Operators	269
4.3.6	Diagonalizing $T(\alpha)$	272
4.3.7	Discussion	275
4.4	The Thermodynamics of the s-d Exchange Model	277
4.4.1	Bethe's Equations for the s-d Exchange Model. Going Over to the Continuous Limit	277
4.4.2	The Equilibrium Distribution	282
4.4.3	The Free Electron Gas ($g \rightarrow 0$ or $S = 0$)	284
4.4.4	Universality	287
4.4.5	The Limits of Strong and Weak Coupling	288
4.4.6	The Thermodynamics of an Impurity	290
4.4.7	Magnetic Susceptibility at $T = 0$ [30, 32, 33]	293
4.4.8	Solution of Equations (4.4.35) and (4.4.36) by an Iterative Method at $T \gg H$ [36, 38] and Perturbation Theory	297
4.4.9	Supplementary Discussion	300
4.5	Solution for the n -fold Degenerate Exchange Model	301
4.5.1	The Bethe Ansatz	301
4.5.2	Magnetic Susceptibility at $T = 0$	303
4.5.3	Thermodynamics	306
4.5.4	Discussion	308
4.6	Conclusion	308
	References	311