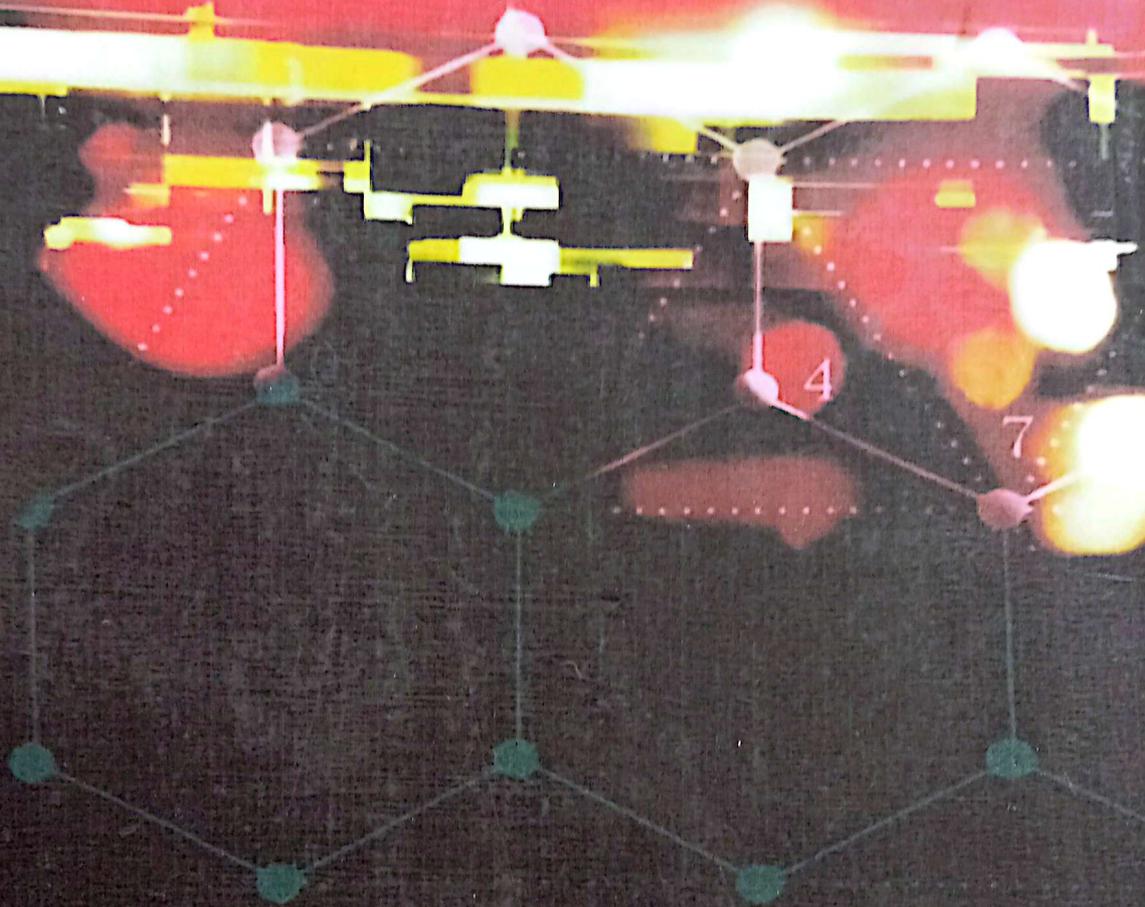


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Methods of **Statistical Physics**

Tomoyasu Tanaka

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more information - www.cambridge.org/9780521580564

CAMBRIDGE UNIVERSITY PRESS

Cambridge, New York, Melbourne, Madrid, Cape Town, Singapore, São Paulo

Cambridge University Press

The Edinburgh Building, Cambridge CB2 2RU, United Kingdom

Published in the United States of America by Cambridge University Press, New York

www.cambridge.org

Information on this title: www.cambridge.org/9780521580564

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First published in print format 2002

ISBN-13 978-0-511-07748-7 eBook (NetLibrary)

ISBN-10 0-511-07748-3 eBook (NetLibrary)

ISBN-13 978-0-521-58056-4 hardback

ISBN-10 0-521-58056-0 hardback

ISBN-13 978-0-521-58958-1 paperback

ISBN-10 0-521-58958-4 paperback

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