

SCHAUM'S
outlines

Vector Analysis

Second Edition

480 fully solved problems

- Complete review of all course fundamentals
- Theories, concepts, and definitions, with an introduction to tensor analysis

USE WITH THESE COURSES

Electromagnetics • Mechanics • Electromagnetic Theory
Aerodynamics

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