

141-4

REAL COMPLEX ANALYSIS

THIRD EDITION

WALTER RUDIN

McGRAW-HILL SERIES IN HIGHER MATHEMATICS

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