

MODEL

CALCULUS AND ANALYTIC GEOMETRY

WITH
MATRICES, DETERMINANTS AND VECTORS

REVISED AND ENLARGED EDITION

FOR CLASS XII



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x

NOTATION

$<$ is less than

$>$ is greater than